

Vector Addition

1.

$$150N + 200N = \underline{350N \text{ E}}$$

2.

$$50N - 63N = -13N \quad \underline{13N \text{ Left}}$$

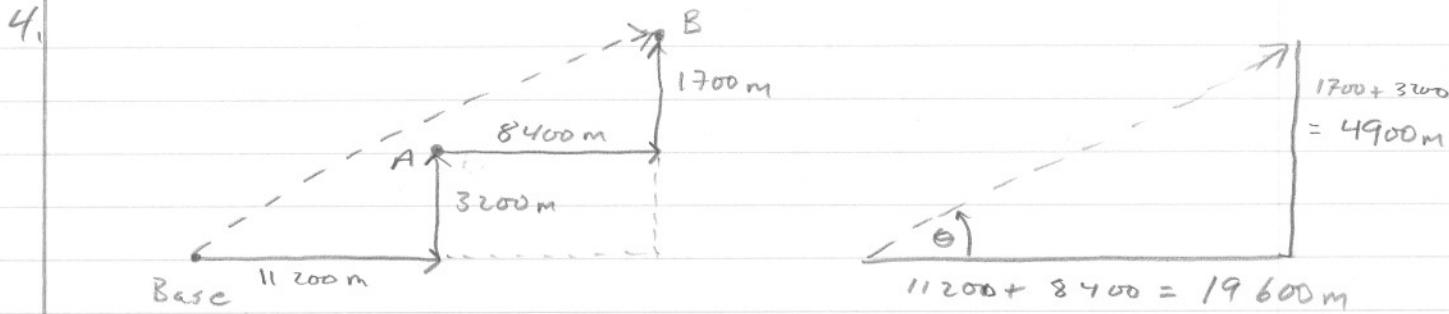
3.

$$\begin{aligned} c^2 &= a^2 + b^2 \\ &= 100^2 + 30^2 \\ &= 10900 \\ c &= \sqrt{10900} = 104.4 \text{ m/s} \end{aligned}$$

$$\tan \theta = \frac{30 \text{ m/s}}{100 \text{ m/s}}$$

$$\theta = \tan^{-1} \left(\frac{30}{100} \right) = 16.699^\circ$$

104 m/s 17° W of N



$$\begin{aligned} (19600 \text{ m})^2 + (4900 \text{ m})^2 &= c^2 \\ 20203 \text{ m} &= c \\ \tan \theta &= \left(\frac{4900 \text{ m}}{19600 \text{ m}} \right) \\ \theta &= 14^\circ \end{aligned}$$

20203 m 14° above the horizontal towards the East

5.

$$c^2 = (52 \text{ m/s})^2 + (12 \text{ m/s})^2$$

$$c = 53.37 \text{ m/s}$$

$$\tan \theta = \frac{12 \text{ m/s}}{52 \text{ m/s}}$$

$$\theta = 12.99^\circ$$

53.4 m/s 13° S of E

6.

$$c^2 = (25 \text{ km})^2 + (35 \text{ km})^2$$

$$c = 43.01 \text{ km}$$

$$\tan \theta = \frac{35 \text{ km}}{25 \text{ km}}$$

$$\theta = 54.46^\circ$$

43.0 km 54.5° S of W

7.

$$c^2 = (12 \text{ m/s})^2 + (6 \text{ m/s})^2$$

$$c = 13.4 \text{ m/s}$$

$$\tan \theta = \frac{6 \text{ m/s}}{12 \text{ m/s}}$$

$$\theta = 26.6^\circ$$

to the shore = $90 - 26.6 = 63.4^\circ$

13.4 m/s 63.4° with respect to the shore

8. (a) $0.8 \text{ miles} + 1.2 \text{ miles} + 0.2 \text{ miles} + 0.4 \text{ miles} = \underline{2.6 \text{ miles}}$

(b)

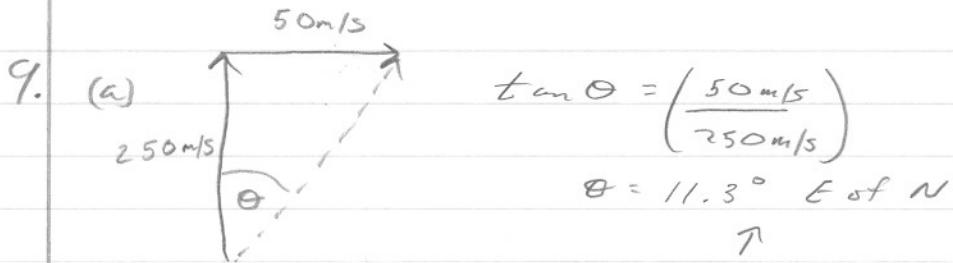
$$c^2 = (.6)^2 + (.8)^2$$

$$c = 1 \text{ mile}$$

$$\tan \theta = \frac{.8}{.6}$$

$$\theta = 53.1^\circ$$

1 mile 53° S of E

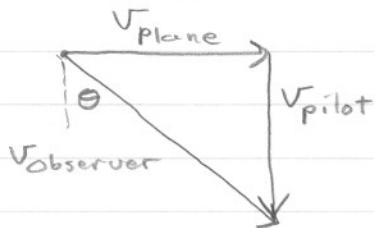


The plane will be pushed this amount
so, the plane must fly at an angle of 11.3° W of N

(b) $c^2 = (50 \text{ m/s})^2 + (250 \text{ m/s})^2$
 $c = 254.95$

The plane's speed with respect to the air will be 255 m/s

10.



$$(v_{\text{Observer}})^2 = (v_{\text{Plane}})^2 + (v_{\text{Pilot}})^2$$

$$(v_{\text{Plane}})^2 = (v_{\text{Observer}})^2 - (v_{\text{Pilot}})^2$$

$$v_{\text{Plane}} = \sqrt{(v_{\text{Observer}})^2 - (v_{\text{Pilot}})^2}$$